

Planetary Atmospheres

Structure

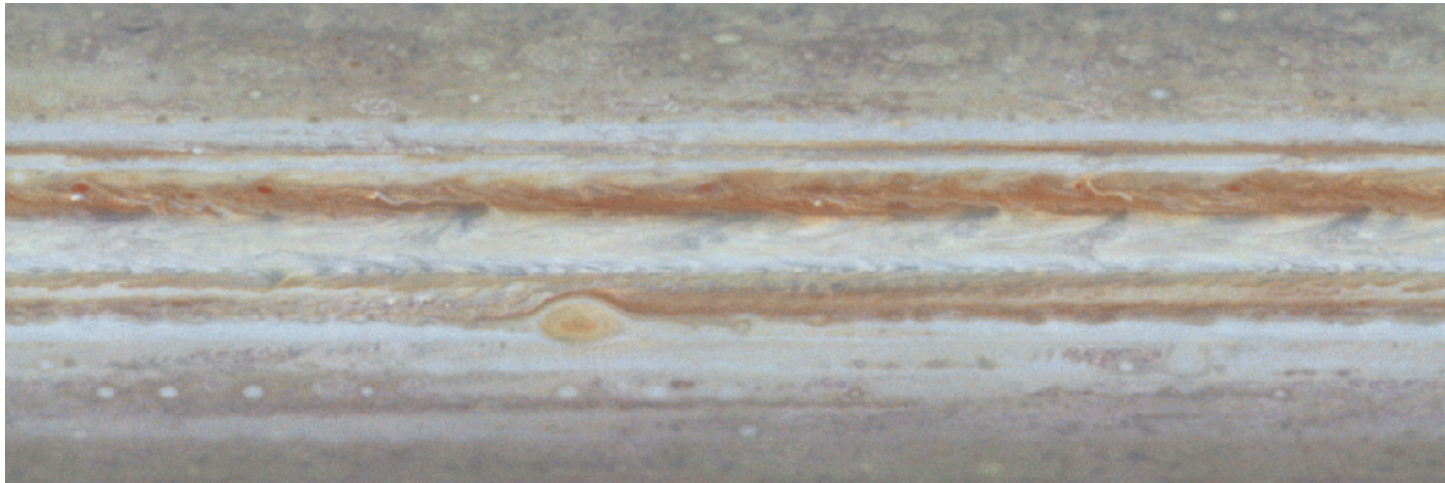
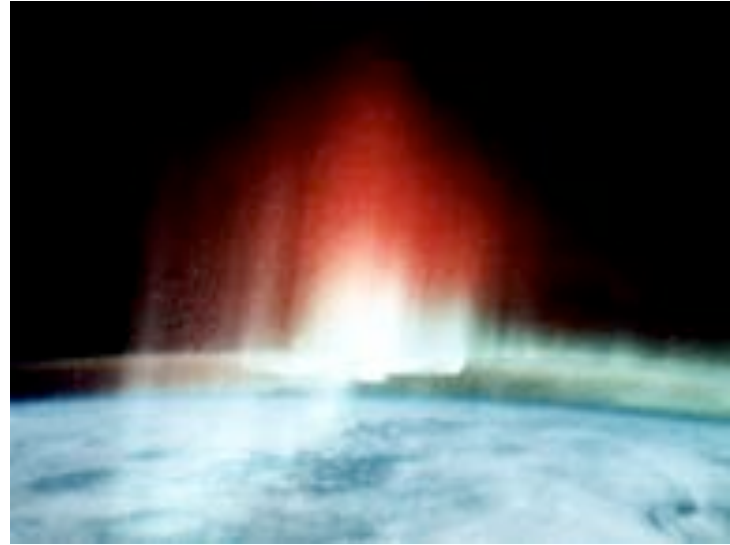
Composition

Clouds

Photochemistry

Meteorology

Atmospheric Escape



Structure

Generalized Hydrostatic Equilibrium

$$P(z) = P(0)e^{-\int_0^z dr / H(r)} \quad \rho(z) = \rho(0)e^{-\int_0^z dr / H^*(r)}$$

Generalized Pressure Scale Height

$$H(z) = \frac{kT(z)}{g_p(z)\mu_a(z)m_{amu}}$$

Generalized Density Scale Height

$$\frac{1}{H^*(z)} = \frac{1}{T(z)} \frac{dT(z)}{dz} + \frac{g_p(z)\mu_a(z)m_{amu}}{kT(z)}$$

Structure

Note: For an Isothermal Atmosphere
(or region of an atmosphere):

$$H(z) = H^*(z)$$

Since $\frac{dT(z)}{dz} = 0$

Remember that $g_p(z) = \frac{GM_p}{r^2} = \frac{GM_p}{(R_p + z)^2}$

* So at small altitudes $r \Rightarrow R_p$ and $g_p(z) \cong g_p(R_p)$

Structure

Most planets have near-surface scale heights ranging between ~10-25 km due to the similar ratios of

$$T/(g_p \mu_a)$$

	Venus	Earth	Mars	Jupiter	Saturn	Uranus	Neptune
T_{surf} (K)	737	288	215	165*	135*	76*	72*
Bond Albedo	0.75	0.31	0.25	0.34	0.34	0.29	0.31
H (km)	16	8.5	11	24	47	25	23

* Temperature at 1 bar pressure

Structure

Of course, temperature actually does vary with height

If a packet of gas rises rapidly (adiabatic), then it will expand and, as a result, cool

Work done in expanding = work done in cooling

$$VdP = \frac{m_{gm}}{\rho} dP \qquad C_p dT$$

m_{gm} is the mass of one mole, ρ is the density of the gas

C_p is the specific heat capacity of the gas at constant pressure

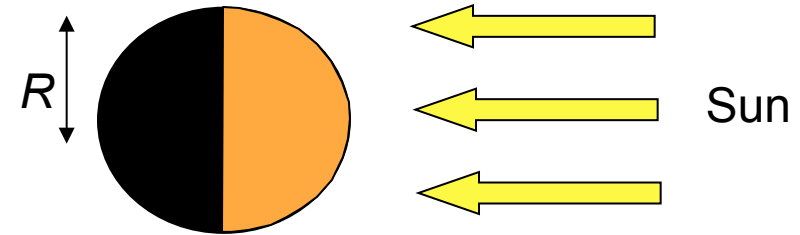
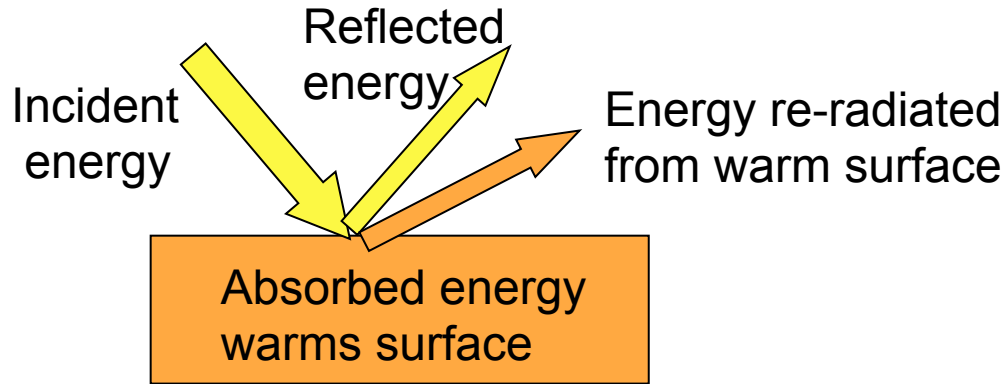
Combining these two equations with hydrostatic equilibrium, we get the dry adiabatic **lapse rate**:

$$\frac{dT}{dz} = \frac{m_{gm} g_p}{C_p} = \frac{g_p}{c_p}$$

* On Earth, the lapse rate is about 10 K/km

Thermal Structure: Surface

What determines a planet's surface temperature?



$$P_{in} = (1 - A_b) \pi R^2 \frac{F_{\odot}}{r_{\odot AU}^2}$$

$$P_{out} = 4\pi R^2 \epsilon \sigma T^4$$

A_b is Bond albedo, F_{\odot} is solar flux at Earth's distance, r_{\odot} is distance of planet to Sun, ϵ is emissivity, σ is Stefan's constant ($5.67 \times 10^{-8} \text{ Wm}^{-2}\text{K}^{-4}$)

Balancing energy in and energy out yields:

$$T_{eq} = \left(\frac{F_{\odot}}{r_{\odot AU}^2} \frac{(1 - A_b)}{4\epsilon\sigma} \right)^{1/4}$$

Thermal Structure: Surface

- Solar constant $F_{\odot} = 1300 \text{ Wm}^{-2}$
- Earth (Bond) albedo $A_b = 0.3$, $\varepsilon = 0.9$
- Equilibrium temperature = 263 K
- How reasonable is this value?

Body	Mercury	Venus	Earth	Mars
A_b	0.12	0.75	0.3	0.25
T_{eq}	446	238	263	216
Actual T	100-725	737	288	215

- How to explain the discrepancies?
- Has the Sun's energy stayed constant with time?